



Elettra Sincrotrone Trieste

# Noise contributions in eBPM systems

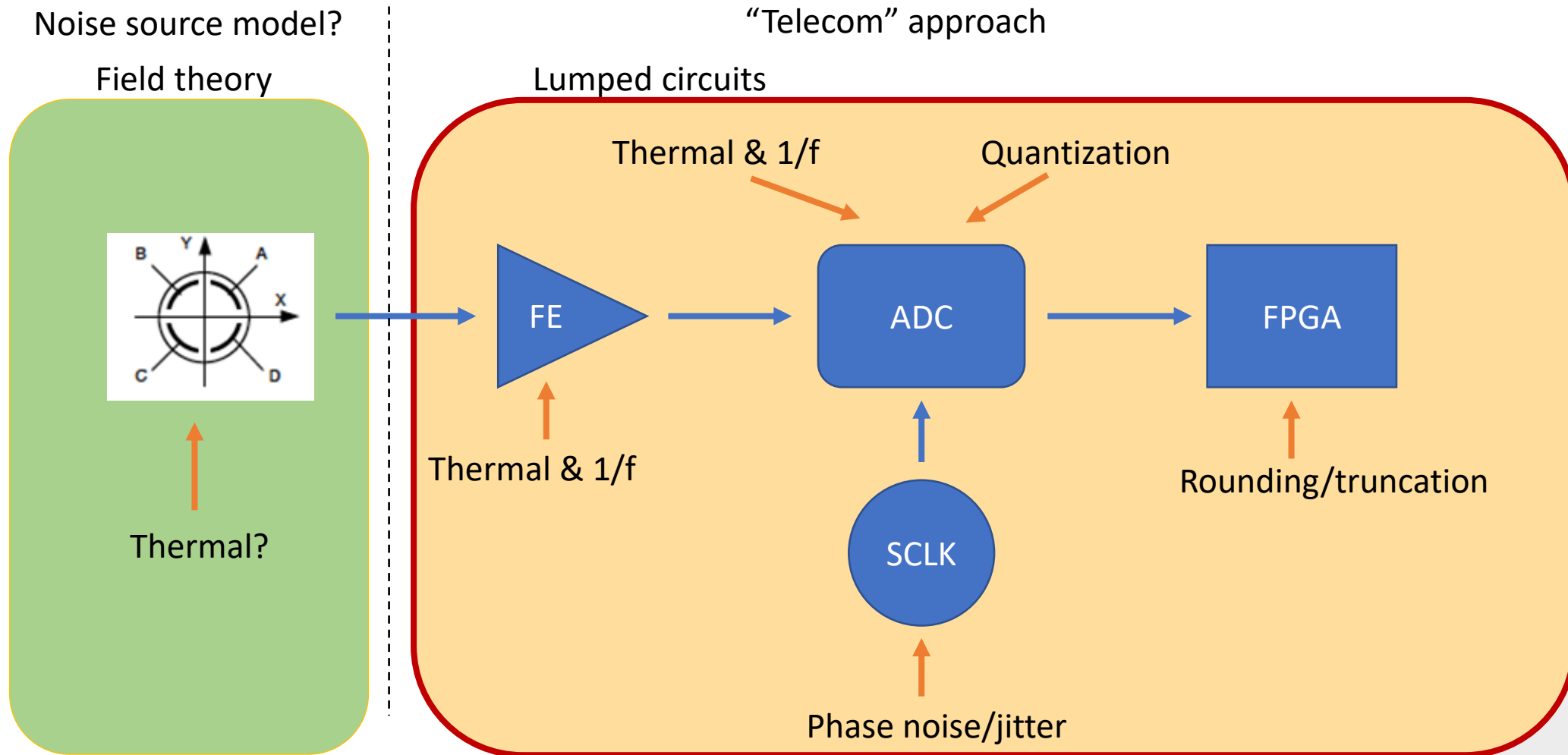
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# Noise in passive/active devices

- We refer as noise as a random process that can be described only through statistical properties, such as:
  - distribution (mean, variance, probability density function)
  - autocorrelation function and its Fourier transform (Power spectral density, PSD)
- Noise power can be estimated integrating the PSD over the given bandwidth

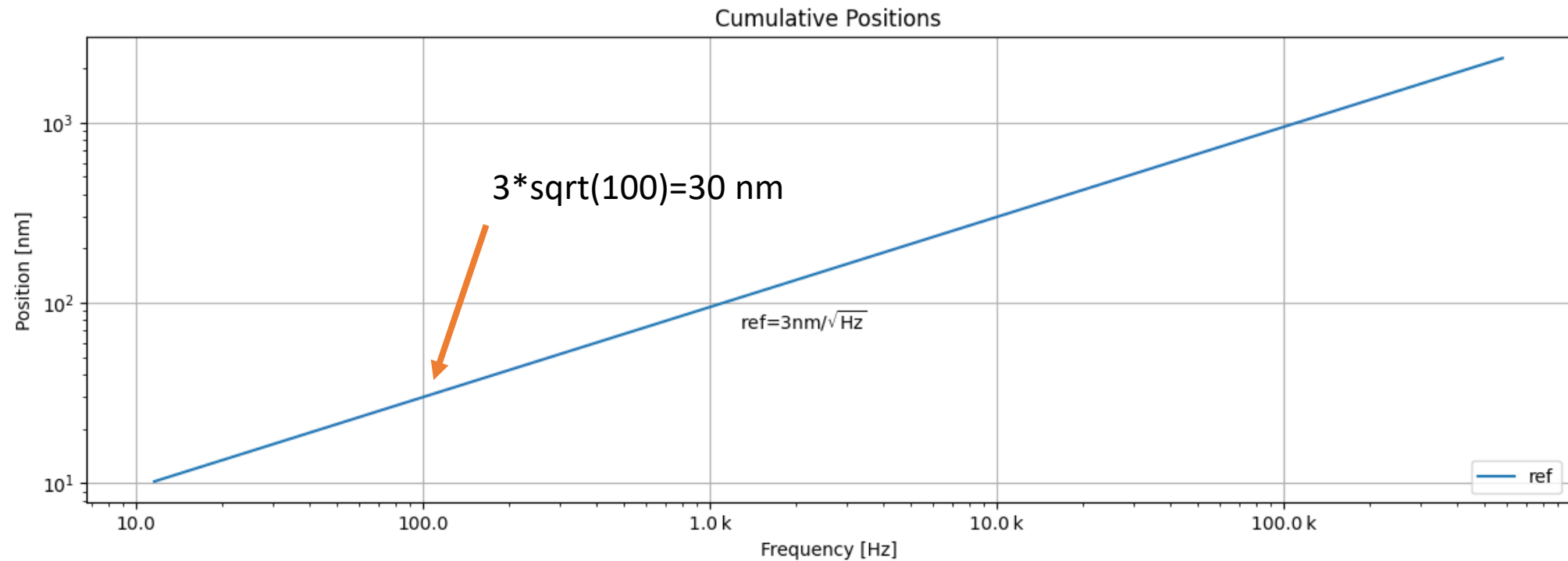
Johnson – Nyquist (thermal)	Shot	Flicker or 1/f
<ul style="list-style-type: none"> <li>• Generated by thermal agitation of charge carriers in a conductor (resistors, channel in a FET, etc)</li> <li>• Usually modelled as a gaussian process</li> <li>• No correlation between samples</li> <li>• <b>PSD is flat</b> (white noise), value is <math>4kTR</math> for voltage noise</li> </ul>	<ul style="list-style-type: none"> <li>• Generated by discrete charge particles that flow across barriers (e.g. p-n junction)</li> <li>• Usually modelled as a Poisson process</li> <li>• No correlation between samples</li> <li>• <b>PSD is flat</b> (white noise), value is <math>2qI</math> for current noise</li> </ul>	<ul style="list-style-type: none"> <li>• Generated by impurities or generation-recombination of charges in electronic devices</li> <li>• Different processes: gaussian or chi-distributed</li> <li>• Correlation between samples</li> <li>• <b>PSD is NOT flat</b>, value is inversely proportional to frequency</li> </ul>

# Noise in BPM acquisition chain



# Noise evaluation in BPMs

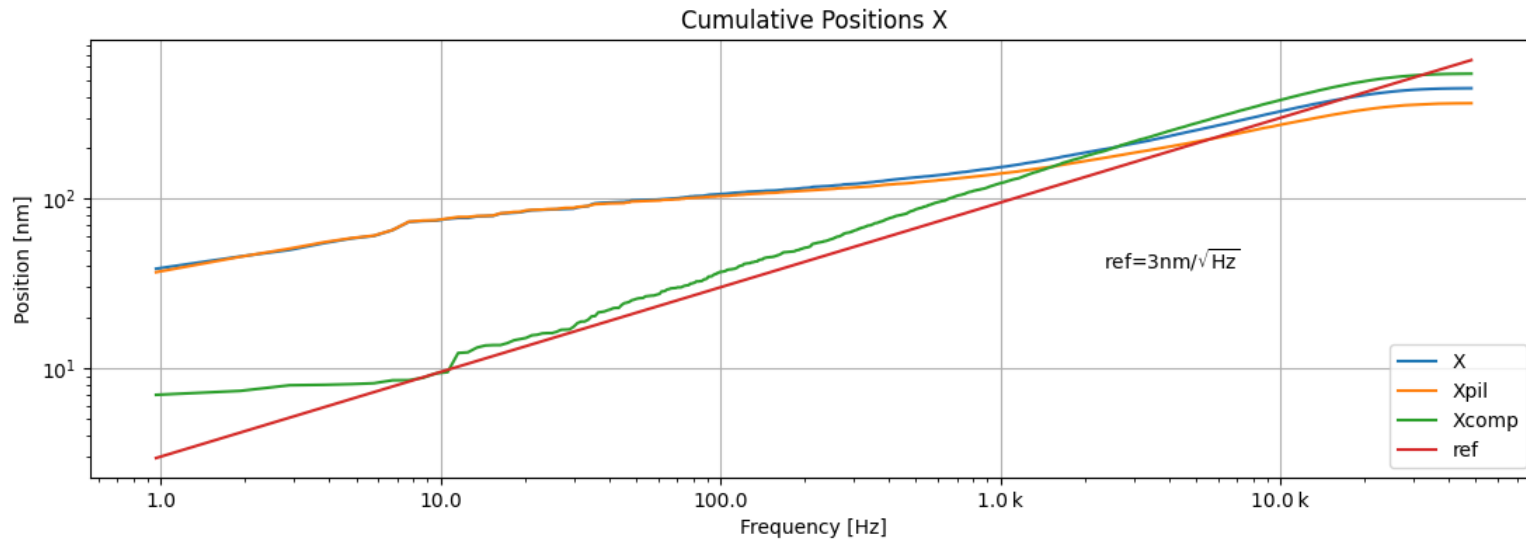
- Easier to refer to noise on calculated positions
- graphs: cumulative sum of PSD vs frequency



# Noise evaluation in BPMs

- Test setup: RF gen + splitter (emulate a stable beam)
- Significant  $1/f$  noise on our BPMs
- Pilot tone compensation can cancel it out
- Coming from ADCs?
  - No difference w & w/o front end -> PTFE has white noise
  - No difference at different frequencies -> not related to sampling clock jitter
  - Could be a ADC “signature”? -> different between various ADC models? (tests in progress)

# Cumulative Spectral Density



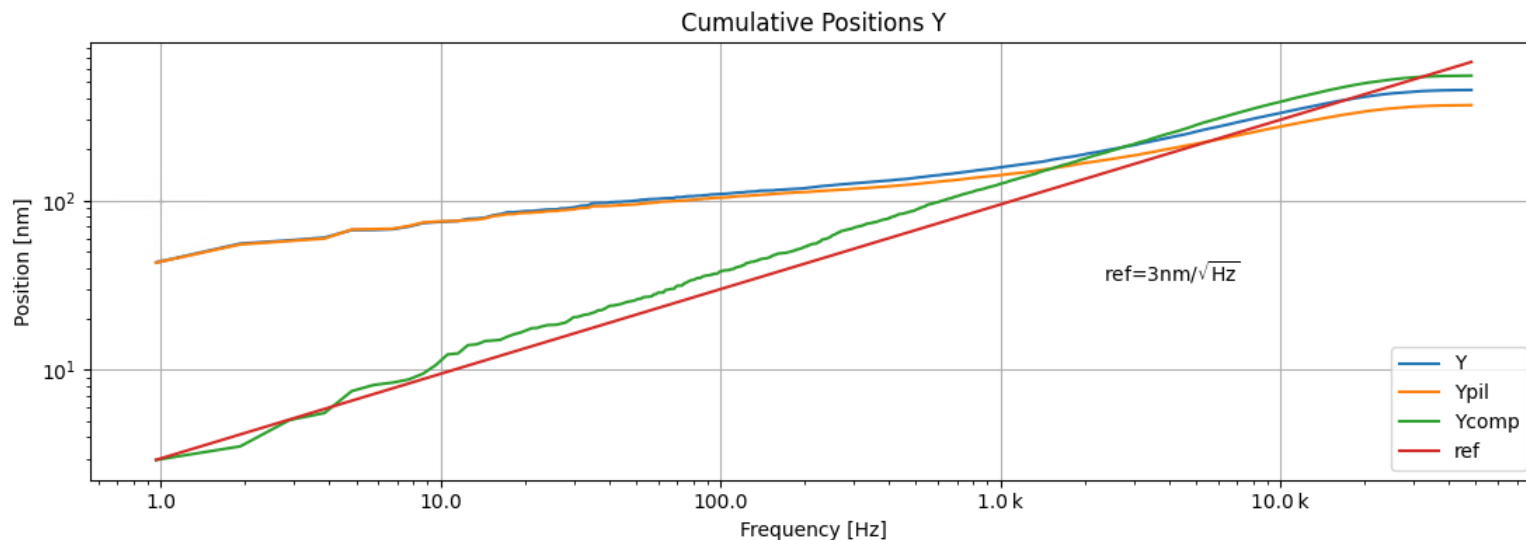
100 kS/s data rate

Red trace: white noise  
reference of 3nm/sqrt(Hz)

Blue trace: carrier

Orange trace: pilot

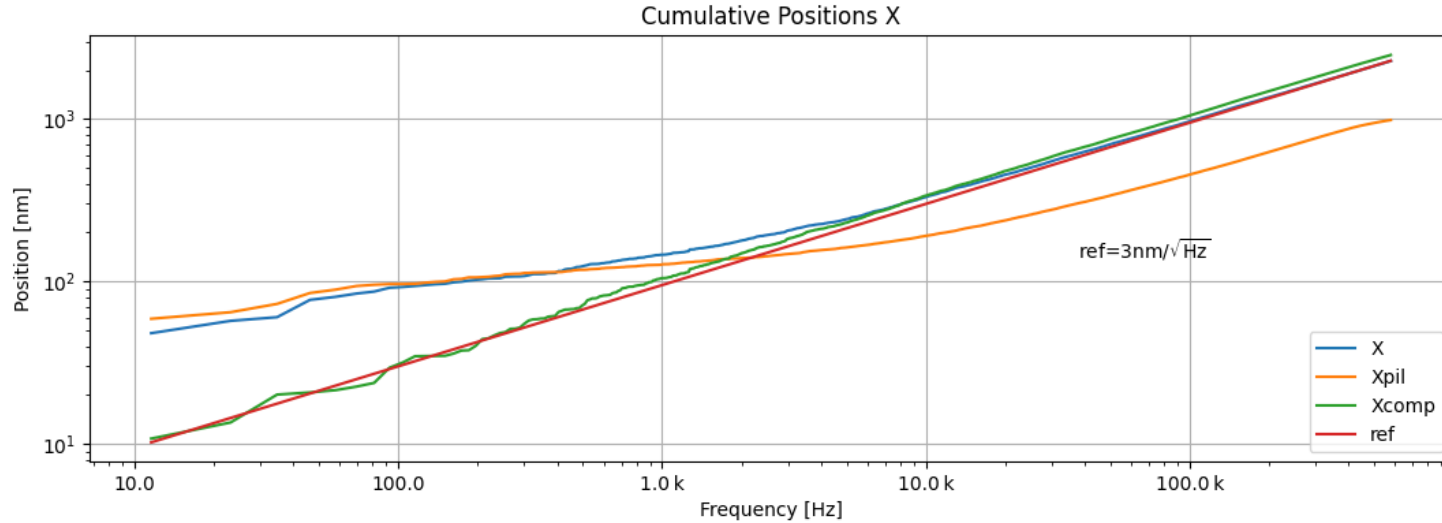
Green trace: compensated  
position



**Noise of non-compensated  
position higher than expected**

Compensated position follows  
theoretical prediction

# Cumulative Spectral Density

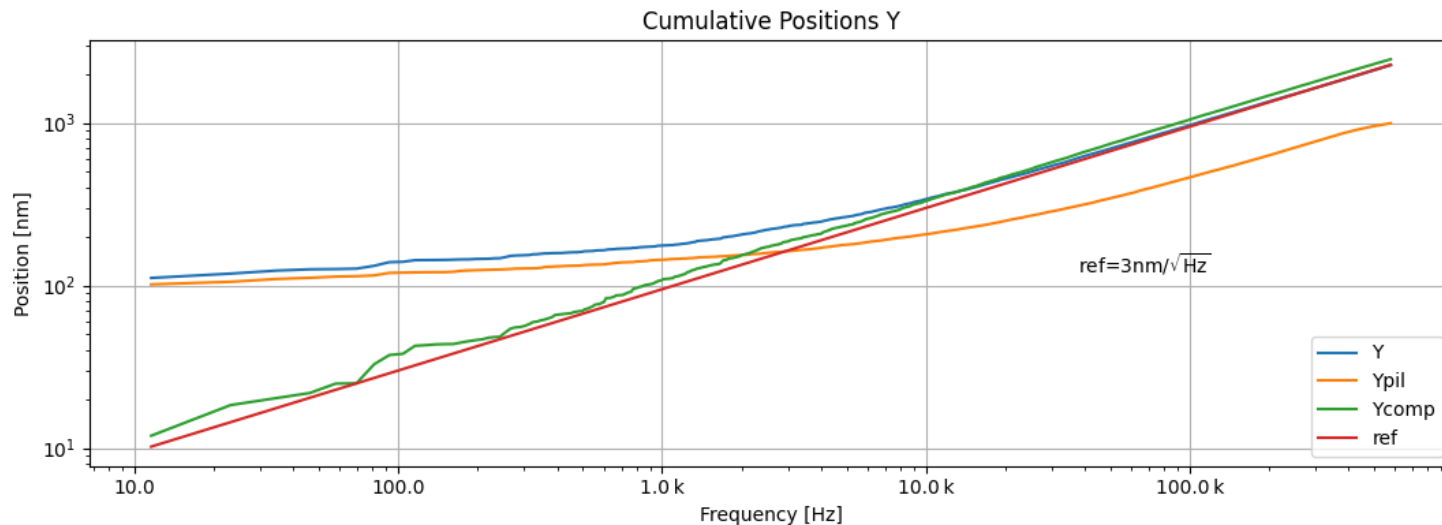


1.156 MS/s data rate - TbT

Noise PSD is flat over 7/10 kHz

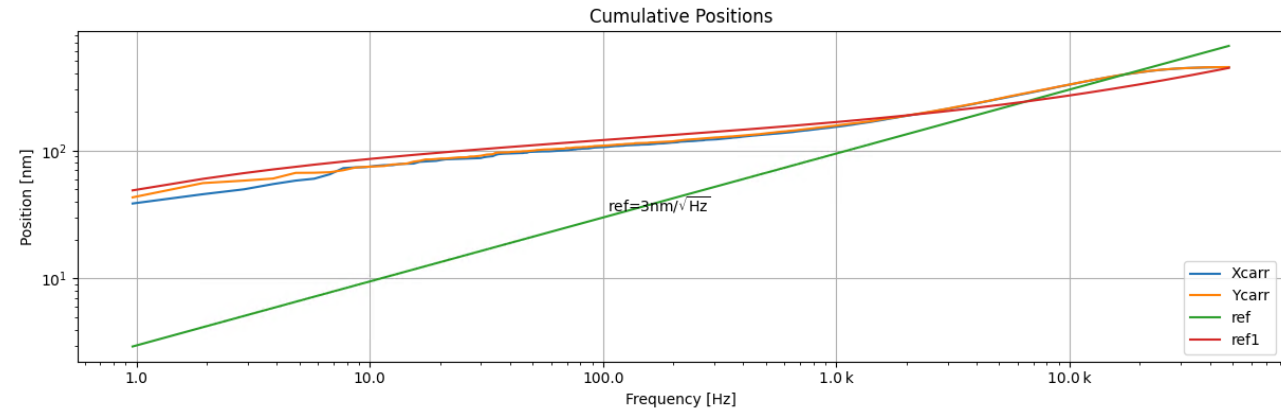
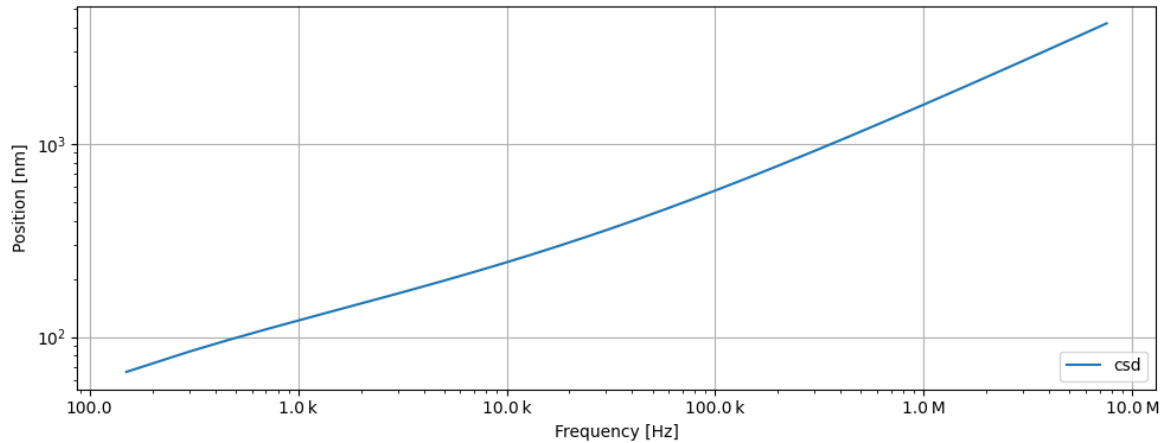
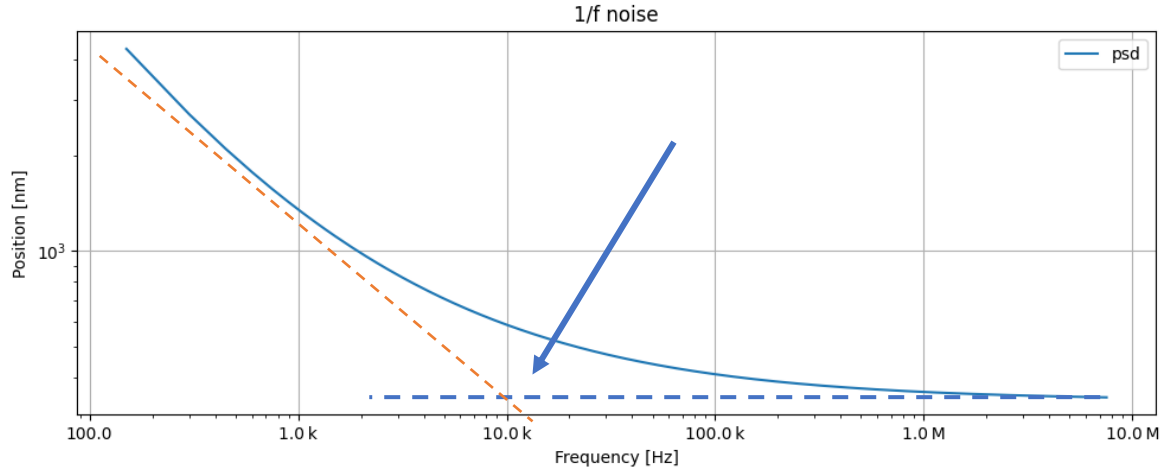
Expanding bandwidth helps to understand the phenomena

Noise on pilot positions is lower due to enhanced filtering (reduced BW)





# 1/f fitting

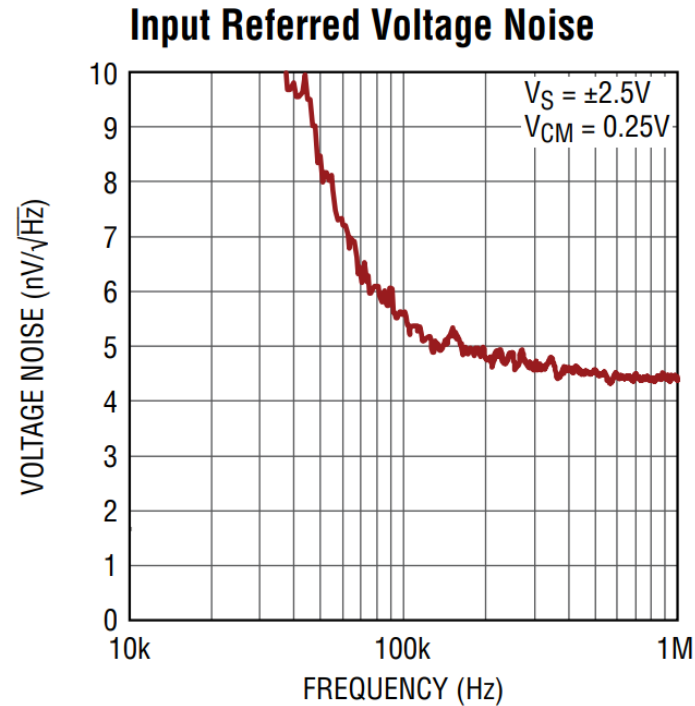
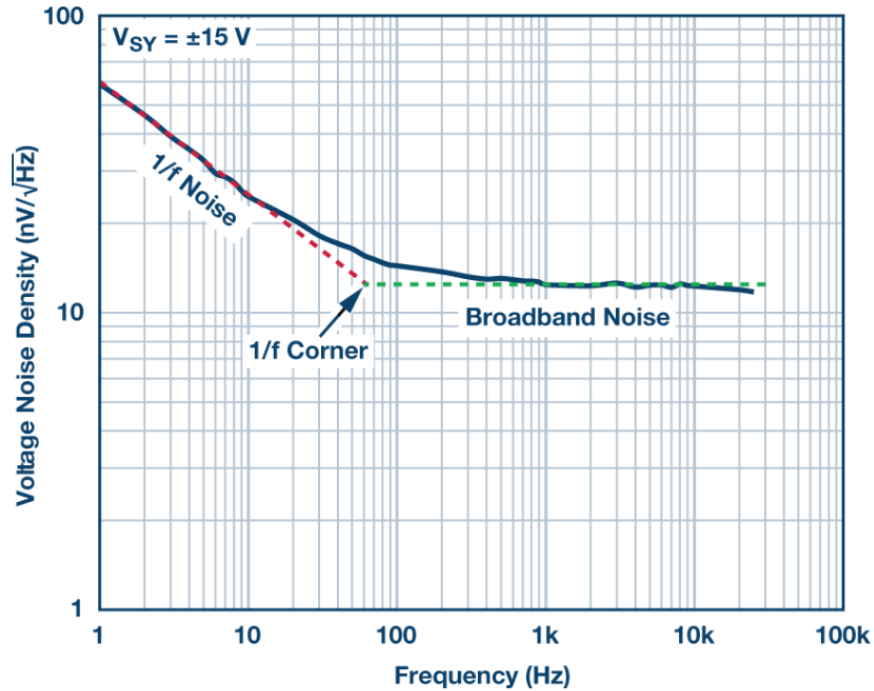


Fit 1/f noise (red trace):

$$\text{PSD: } S(f) = \frac{k^2 F_c}{f} + k^2, \quad k = 3\text{nm}/\sqrt{\text{Hz}}$$

Corner frequency: about 10 kHz

# Examples of 1/f noise in opamps



6268 G16

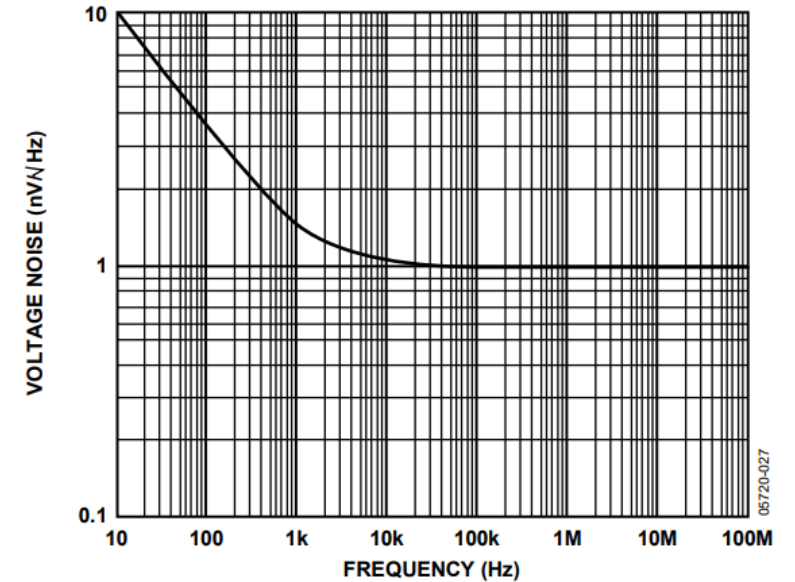
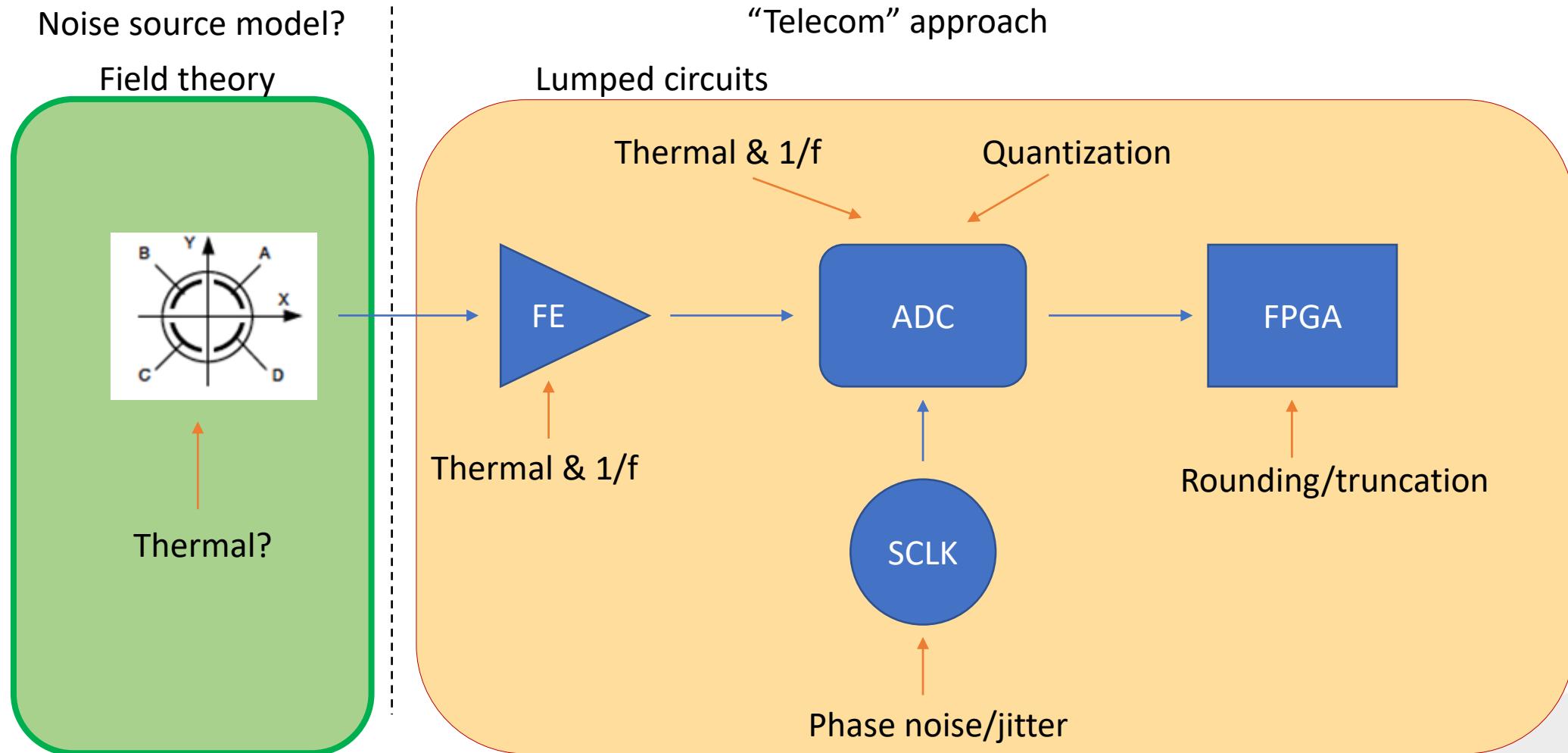


Figure 13. Voltage Noise vs. Frequency

# Noise in BPM acquisition chain

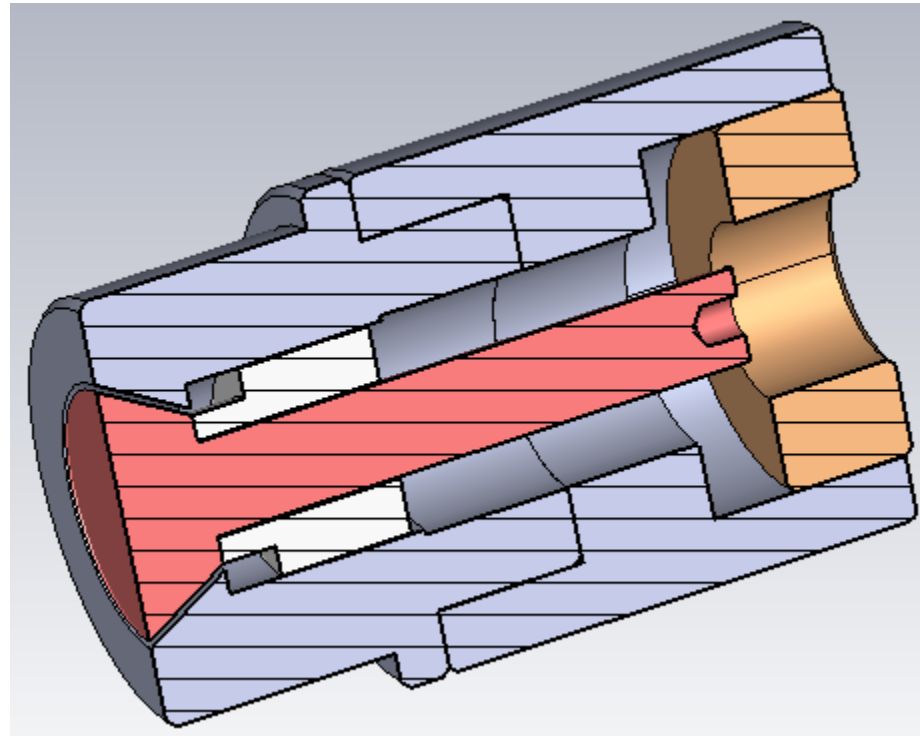


# S/N and position resolution

- Measurements are limited by (thermal) noise
- Signal power: TEM mode propagation implies that voltage and current concepts for lumped circuits can be defined at the signal port of the Pickup
- Noise power: what kind of electric source model matches the Pickup?
- Several articles/papers assume a thermal noise generator (Thevenin equivalent circuit)
- Thermal movement of electrons, independently from each other, in conducting material ( $\sigma > 0$ )

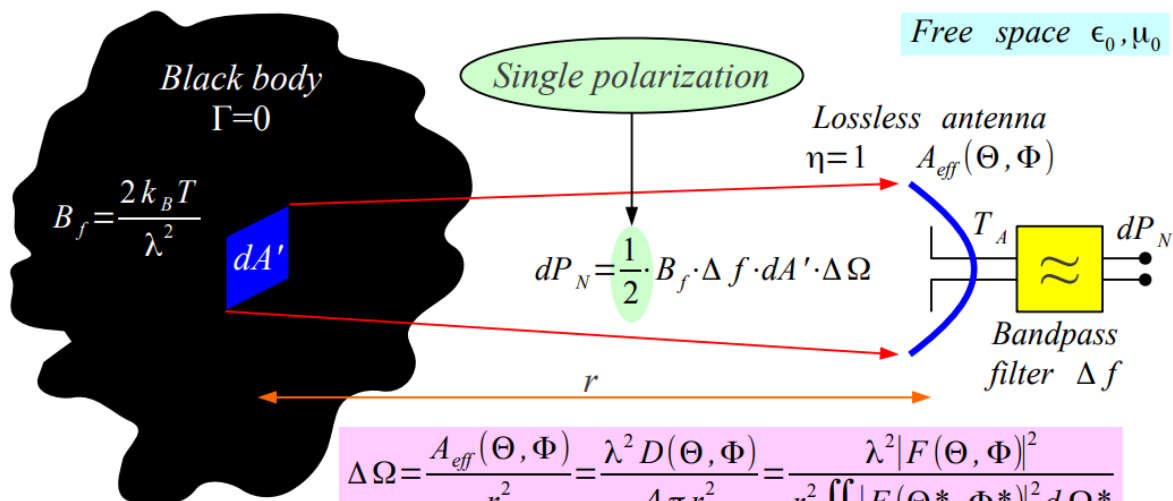
# Button type pickup

- Button type PU: what is R? How a coaxial propagation path can be modeled as a noise source?



# Antenna theory

- Some references (M. Vidmar, Noise in Radio/Optical Communications, IBIC 2108; thanks to B. Roche for pointing it out)



$$\Delta\Omega = \frac{A_{eff}(\theta, \Phi)}{r^2} = \frac{\lambda^2 D(\theta, \Phi)}{4\pi r^2} = \frac{\lambda^2 |F(\theta, \Phi)|^2}{r^2 \iint_{4\pi} |F(\theta^*, \Phi^*)|^2 d\Omega^*}$$

$$dA' = r^2 d\Omega$$

$$P_N = \iint_{A'} \frac{1}{2} B_f \cdot \Delta f \cdot dA' \cdot \Delta\Omega = \iint_{4\pi} \frac{1}{2} \cdot \frac{2k_B T(\theta, \Phi)}{\lambda^2} \cdot \Delta f \cdot r^2 d\Omega \cdot \frac{\lambda^2 |F(\theta, \Phi)|^2}{r^2 \iint_{4\pi} |F(\theta^*, \Phi^*)|^2 d\Omega^*}$$

$$P_N = \Delta f k_B \frac{\iint_{4\pi} T(\theta, \Phi) |F(\theta, \Phi)|^2 d\Omega}{\iint_{4\pi} |F(\theta, \Phi)|^2 d\Omega} = \Delta f k_B T_A$$

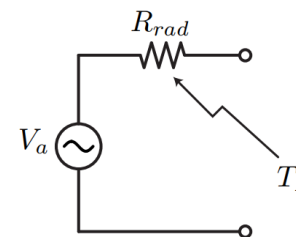
$$T_A = \frac{\iint_{4\pi} T(\theta, \Phi) |F(\theta, \Phi)|^2 d\Omega}{\iint_{4\pi} |F(\theta, \Phi)|^2 d\Omega}$$

4 – Received thermal-noise power

Power radiated by a physical object:  $P_N = kT_N B$

Power collected by a **lossless** antenna:  $P_A = S A_e B = kT_A B$ , depends on solid angles of source and receiver (radiation pattern) -  $T_A$  is **not related** to physical temperature of the antenna

Equivalent noise circuit: we shall consider the radiation resistance of the antenna (ratio between E and H):

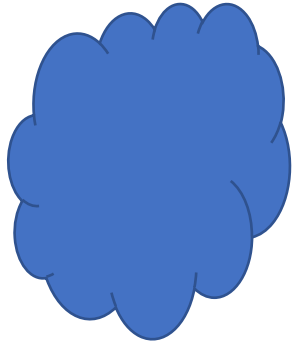


$$V_a^2(f) = 4kT_A R_{rad} B$$

With matched load:  $P_L = kT_A B = P_A$

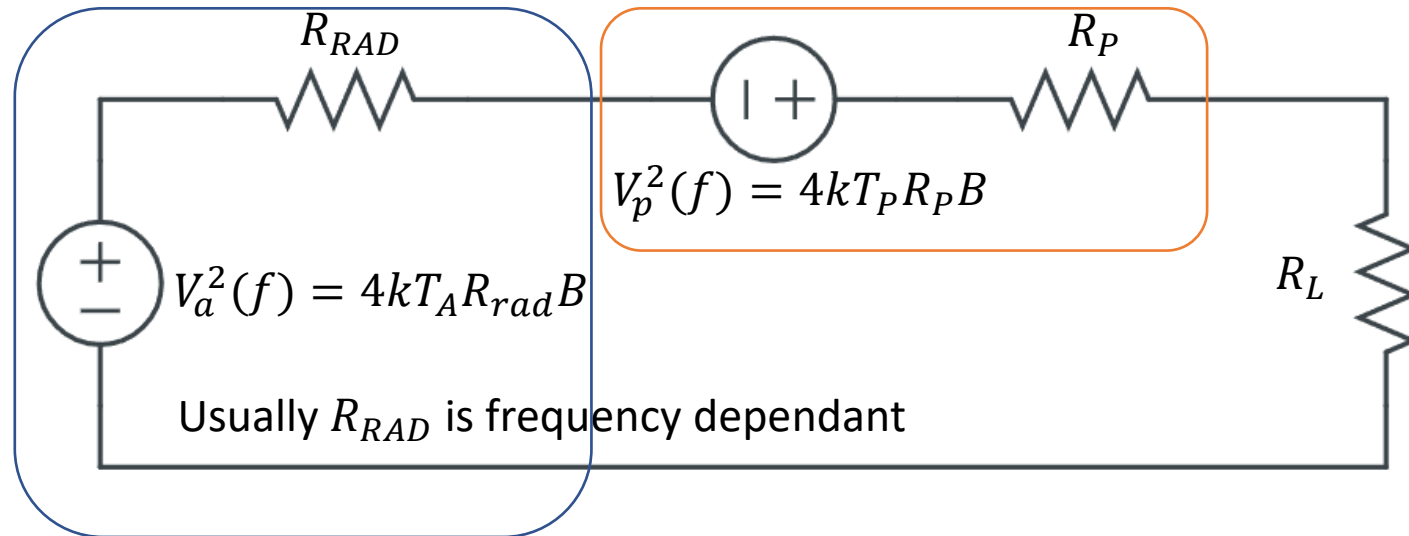
# Pickup – proposed equivalent circuit

Vacuum chamber  
(is it radiating  
noise power? At  
which  
temperature?  $T_C$ )



Pickup (antenna with  
a narrow directivity,  
 $T_A$  and a given  $R_{RAD}$ )

Pickup losses from  
conductor and  
dielectric?  $T_P$ ?



Load impedance –  
usually very  
different from  
 $R_{RAD}$  (coax cable  
omitted)

Voltage noise on  $R_L$ : 
$$V_L^2 = V_a^2 \left( \frac{R_L}{R_L + R_{RAD} + R_P} \right)^2 + V_p^2 \left( \frac{R_L}{R_L + R_{RAD} + R_P} \right)^2$$

Depends on:

- Temperatures (real and equivalent)
- Ratio between impedances

# Thermal noise standards (NIST)

- Johnson noise thermometry based on available power:  $T = Pa/kB$
- The power density is assumed constant in the measurement bandwidth
- For the evaluation of the noise along the BPM acquisition chain a coaxial thermal noise generator could be used as noise source.



# Questions

- Have you ever observed 1/f noise on calculated positions from BPMs? Could you define a clear “electronic” source?
- How can be modelled the noise from the pickups? Or can they be considered “noiseless” at the end?
  - References in “traditional” articles/papers take for granted the thermal noise behaviour with matched impedances (available power  $P=kTB$ )

# Thank you!





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